

# *Precision $\beta$ -Decay Studies in the LHC Era*

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The Standard Model, successful though it may be, leaves many questions unanswered.

Yet the only compelling evidence we have for physics beyond the SM from **terrestrial experiments** is that **neutrinos have mass**.

### Some Basic Questions, circa 2007

- How well has the Standard Model been tested?
- How well should we have to test it to find “new physics”?
- Does the specific nature of the new physics we know constrain what we don't know? Really?
- Does the LHC make the low energy searches for new physics moot?

# How well has the Standard Model been tested?

Tests exist in different sectors...

## 1. Precision Electroweak.

Quantity	Value	Standard Model	Pull
$m_e$ [GeV]	$172.7 \pm 2.9 \pm 0.6$	$172.7 \pm 2.8$	0.0
$M_W$ [GeV]	$80.450 \pm 0.058$	$80.376 \pm 0.017$	1.3
	$80.392 \pm 0.039$		0.4
$M_Z$ [GeV]	$91.1876 \pm 0.0021$	$91.1874 \pm 0.0021$	0.1
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	$2.4968 \pm 0.0011$	-0.7
$\Gamma(\text{had})$ [GeV]	$1.7444 \pm 0.0020$	$1.7434 \pm 0.0010$	—
$\Gamma(\text{inv})$ [MeV]	$499.0 \pm 1.5$	$501.85 \pm 0.11$	—
$\Gamma(\tau^+\tau^-)$ [MeV]	$83.984 \pm 0.086$	$83.996 \pm 0.021$	—
$\sigma_{\text{had}}$ [nb]	$41.541 \pm 0.037$	$41.467 \pm 0.009$	2.0
$R_e$	$20.804 \pm 0.050$	$20.756 \pm 0.011$	1.0
$R_\mu$	$20.785 \pm 0.033$	$20.756 \pm 0.011$	0.9
$R_\tau$	$20.764 \pm 0.045$	$20.801 \pm 0.011$	-0.8
$R_b$	$0.21029 \pm 0.00066$	$0.21578 \pm 0.00010$	0.8
$R_c$	$0.1721 \pm 0.0030$	$0.17230 \pm 0.00094$	-0.1
$A_{FB}^{(0,e)}$	$0.0145 \pm 0.0025$	$0.01622 \pm 0.00025$	-0.7
$A_{FB}^{(0,\mu)}$	$0.0169 \pm 0.0013$		0.5
$A_{FB}^{(0,\tau)}$	$0.0188 \pm 0.0017$		1.5
$A_{FB}^{(0,b)}$	$0.0992 \pm 0.0016$	$0.1031 \pm 0.0008$	-2.4
$A_{FB}^{(0,c)}$	$0.0707 \pm 0.0035$	$0.0737 \pm 0.0006$	-0.8
$A_{FB}^{(0,s)}$	$0.0976 \pm 0.0114$	$0.1032 \pm 0.0008$	-0.5
$\hat{s}_B^2(A_{FB}^{(0,q)})$	$0.2324 \pm 0.0012$	$0.23152 \pm 0.00014$	0.7
	$0.2238 \pm 0.0050$		-1.5
$A_e$	$0.15138 \pm 0.00216$	$0.1471 \pm 0.0011$	2.0
	$0.1544 \pm 0.0060$		1.2
	$0.1498 \pm 0.0049$		0.6
$A_\mu$	$0.142 \pm 0.015$		-0.3
$A_\tau$	$0.136 \pm 0.015$		-0.7
	$0.1439 \pm 0.0043$		-0.7
$A_b$	$0.923 \pm 0.020$	$0.9347 \pm 0.0001$	-0.6
$A_c$	$0.670 \pm 0.027$	$0.6678 \pm 0.0005$	0.1
$A_s$	$0.895 \pm 0.091$	$0.9356 \pm 0.0001$	-0.4
$\hat{s}_B^2$	$0.30005 \pm 0.00137$	$0.30378 \pm 0.00021$	-2.7
$\hat{s}_B^2$	$0.03076 \pm 0.00110$	$0.03006 \pm 0.00003$	0.6
$\hat{s}_B^2$	$-0.040 \pm 0.015$	$-0.0396 \pm 0.0003$	0.0
$\hat{s}_A^2$	$-0.507 \pm 0.014$	$-0.5064 \pm 0.0001$	0.0
$A_{PV}$	$-1.31 \pm 0.17$	$-1.53 \pm 0.02$	1.3
$Q_W(\text{Ce})$	$-72.82 \pm 0.46$	$-73.17 \pm 0.03$	1.2
$Q_W(\text{Tl})$	$-116.6 \pm 3.7$	$-116.78 \pm 0.05$	0.1
$\frac{\Gamma(\text{had})}{\Gamma(\text{had}+\tau)}$	$3.35^{+0.20}_{-0.44} \times 10^{-3}$	$(3.22 \pm 0.09) \times 10^{-3}$	0.3
$\frac{\Gamma(\text{had}+\tau)}{\Gamma(\text{had}+\tau)+\Gamma(\text{had})}$	$4511.07 \pm 0.82$	$4509.82 \pm 0.10$	1.5
$r_e$ [%]	$290.89 \pm 0.28$	$291.87 \pm 1.76$	-0.4

## 2. Precision QED (& QCD).

G. Gabrielse, D. Hanneke, T. Kinoshita, M. Nio, and B. Odom, *New Determination of the Fine Structure Constant from the Electron  $g$  Value and QED*, PRL **97**, 030802 (2006).

Quantum electrodynamics (QED) predicts a

relationship between the dimensionless magnetic

moment of the electron ( $g$ ) and the fine structure

constant ( $\alpha$ ). A new measurement of  $g$  using a

one-electron quantum cyclotron, together with a QED

calculation involving 891 eighth-order Feynman

diagrams, determine  $\alpha^{-1} = 137.035 999 710 (96)$

[0.70 ppb]....

## 3. Precision Flavor Physics.

Enter the CKM matrix...

# The Cabibbo-Kobayashi-Maskawa (CKM) Matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{\text{weak}} = V_{\text{CKM}} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{mass}} \quad ; \quad V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

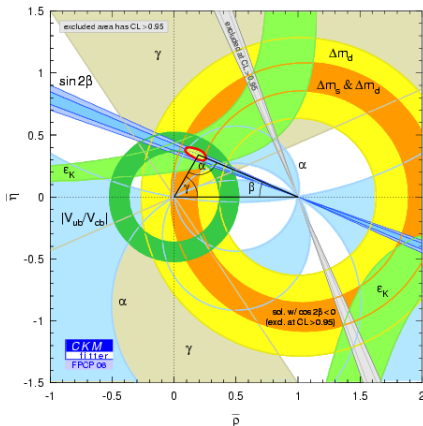
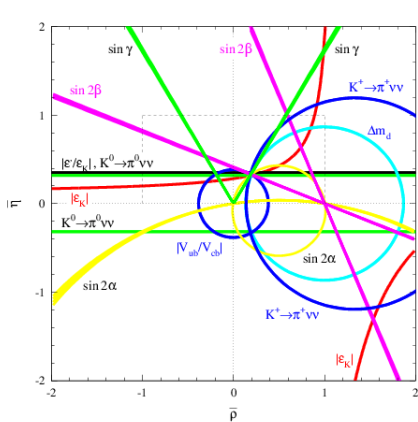
In the **Wolfenstein parametrization (1983)**

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

where  $\lambda \equiv |V_{us}| \simeq 0.22$  and is thus “small”.  $A, \rho, \eta$  are real.

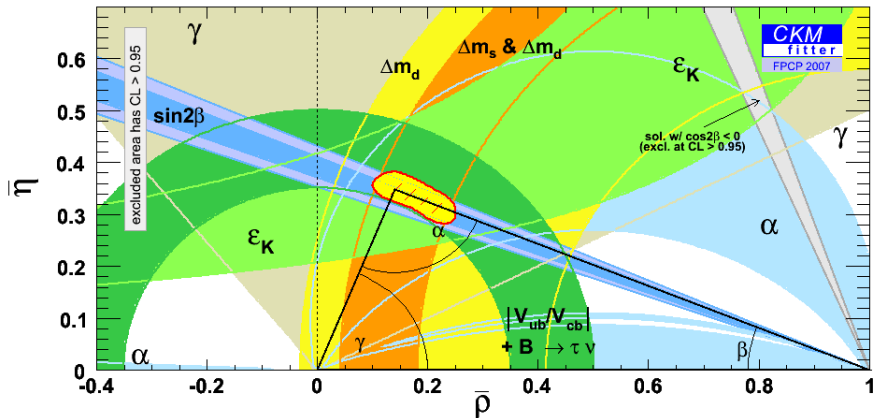
- There are three “generations” of particles.  
Thus, the CKM matrix is unitary [ $V_{\text{CKM}}^\dagger V_{\text{CKM}} = 1$ ]
- The unitarity of the CKM matrix and the structure of the weak currents implies that four parameters capture the CKM matrix.
- A real, orthogonal  $3 \times 3$  matrix contains three parameters. The fourth parameter ( $\eta$ ) must make  $V_{\text{CKM}}$  complex.
- All CP-violating phenomena are encoded in  $\eta$ .

# Testing CKM Unitarity – “the” Unitarity Triangle



[CKMfitter: hep-ph/0104062, hep-ph/0406184 ; <http://ckmfitter.in2p3.fr> – April, 2006 update]

# Testing CKM Unitarity – “the” Unitarity Triangle

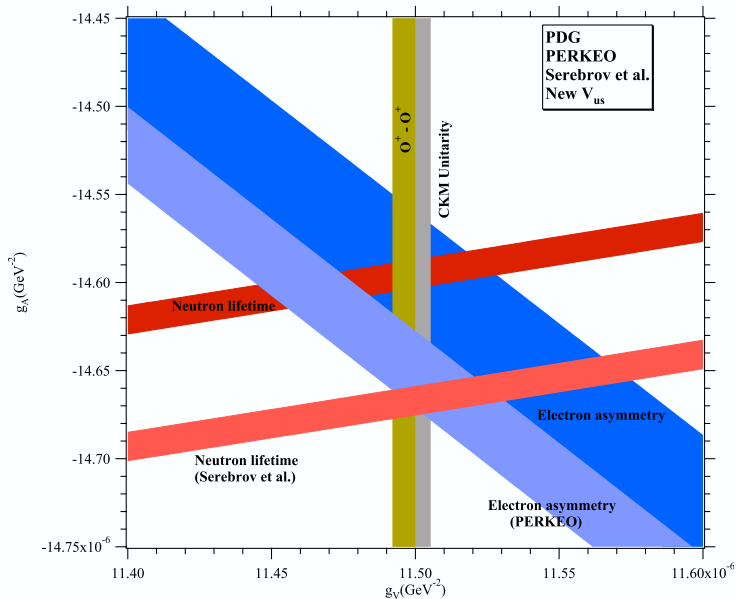


[CKMfitter: hep-ph/0104062, hep-ph/0406184 ; <http://ckmfitter.in2p3.fr> – June, 2007 update]

# Testing the CKM Paradigm

Observable	central $\pm$ C.L. $\equiv 1\sigma$	$\pm$ C.L. $\equiv 2\sigma$	$\pm$ C.L. $\equiv 3\sigma$
$ V_{ud} $	$0.97383^{+0.00024}_{-0.00023}$	$+0.00047$ $-0.00047$	$+0.00071$ $-0.00071$
$ V_{us} $	$0.2272^{+0.0010}_{-0.0010}$	$+0.0020$ $-0.0020$	$+0.0030$ $-0.0030$
$ V_{ub} $ [ $10^{-3}$ ]	$3.82^{+0.15}_{-0.15}$	$+0.31$ $-0.29$	$+0.49$ $-0.44$
$ V_{ub} $ [ $10^{-3}$ ] (meas. not in fit)	$3.64^{+0.19}_{-0.18}$	$+0.39$ $-0.36$	$+0.60$ $-0.55$
$ V_{cd} $	$0.22712^{+0.00099}_{-0.00103}$	$+0.00199$ $-0.00205$	$+0.00300$ $-0.00307$
$ V_{cs} $	$0.97297^{+0.00024}_{-0.00023}$	$+0.00048$ $-0.00047$	$+0.00071$ $-0.00071$
$ V_{cb} $ [ $10^{-3}$ ]	$41.79^{+0.63}_{-0.63}$	$+1.26$ $-1.27$	$+1.89$ $-1.90$
$ V_{cb} $ [ $10^{-3}$ ] (meas. not in fit)	$44.9^{+1.2}_{-2.8}$	$+2.4$ $-5.7$	$+3.8$ $-7.7$
$ V_{td} $ [ $10^{-3}$ ]	$8.28^{+0.33}_{-0.29}$	$+0.92$ $-0.57$	$+1.38$ $-0.86$
$ V_{ts} $ [ $10^{-3}$ ]	$41.13^{+0.63}_{-0.62}$	$+1.25$ $-1.24$	$+1.87$ $-1.86$
$ V_{tb} $	$0.999119^{+0.000026}_{-0.000027}$	$+0.000052$ $-0.000054$	$+0.000078$ $-0.000082$
$ V_{td}/V_{ts} $	$0.2011^{+0.0081}_{-0.0065}$	$+0.0230$ $-0.0127$	$+0.0345$ $-0.0195$
$ V_{ud}V_{ub}^* $ [ $10^{-3}$ ]	$3.72^{+0.15}_{-0.14}$	$+0.30$ $-0.29$	$+0.48$ $-0.43$
$\arg[V_{ud}V_{ub}^*]$ (deg)	$59.8^{+4.9}_{-4.0}$	$+13.9$ $-7.8$	$+20.9$ $-12.1$
$\arg[-V_{ts}V_{tb}^*]$ (deg)	$1.043^{+0.061}_{-0.057}$	$+0.151$ $-0.114$	$+0.238$ $-0.176$
$ V_{cd}V_{cb}^* $ [ $10^{-3}$ ]	$9.49^{+0.15}_{-0.15}$	$+0.30$ $-0.30$	$+0.45$ $-0.45$
$\arg[-V_{cd}V_{cb}^*]$ (deg)	$0.0339^{+0.0021}_{-0.0020}$	$+0.0050$ $-0.0040$	$+0.0077$ $-0.0060$
$ V_{td}V_{tb}^* $ [ $10^{-3}$ ]	$8.27^{+0.33}_{-0.29}$	$+0.93$ $-0.57$	$+1.38$ $-0.85$
$\arg[V_{td}V_{tb}^*]$ (deg)	$-22.84^{+1.00}_{-0.99}$	$+1.98$ $-2.02$	$+2.93$ $-3.21$
$\sin\theta_{12}$	$0.2272^{+0.0010}_{-0.0010}$	$+0.0020$ $-0.0020$	$+0.0030$ $-0.0030$
$\sin\theta_{13}$ [ $10^{-3}$ ]	$3.82^{+0.15}_{-0.15}$	$+0.31$ $-0.30$	$+0.49$ $-0.44$
$\sin\theta_{23}$ [ $10^{-3}$ ]	$41.78^{+0.63}_{-0.63}$	$+1.26$ $-1.26$	$+1.90$ $-1.89$

Table 3: Numerical results of the global CKM fit (II) [51]. The errors correspond to one, two and three standard deviations, respectively.



## Using the global fits...

The first row of the CKM matrix yields the most precise test of CKM unitarity:

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9992 \pm 0.0011$$

whereas

$$|V_{ud}|^2 + |V_{cd}|^2 + |V_{td}|^2 = 1.001 \pm 0.005$$

$$|V_{cd}|^2 + |V_{cs}|^2 + |V_{cb}|^2 = 0.968 \pm 0.181$$

N.B. the  $W$  leptonic width and the  $V_{ud}$  unitarity test (1<sup>st</sup> row) yields

$$|V_{cd}|^2 + |V_{cs}|^2 + |V_{cb}|^2 = 1.003 \pm 0.027$$

cf.  $\alpha + \beta + \gamma = 184_{-15}^{+20}^\circ$ .

[“The CKM Quark-Mixing Matrix,” PDG, 2006.]

**Tests to this precision require precise computations of SM radiative corrections...**

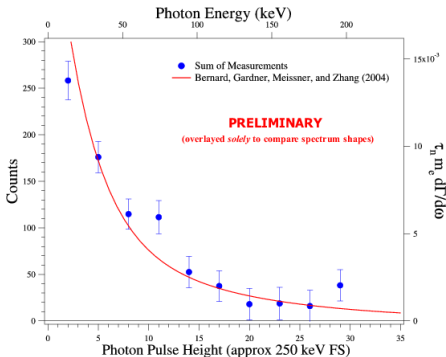
$$g_V = V_{ud}(1 + \Delta\hat{r}_\beta - \Delta\hat{r}_\mu)$$

The precision of the current unitarity tests probes the reliability of these computations to the sub-1% level.

# Testing SM radiative corrections

SM radiative corrections relate the vector weak coupling constant  $g_V$  of the nucleon to  $V_{ud}$ .

The decay  $n \rightarrow pe^- \bar{\nu}_e \gamma$  has finally been observed.



For  $\omega \in [0.015 \text{ MeV}, 0.340 \text{ MeV}]$  we find a Br of  $2.85 \cdot 10^{-3}$ , cf. with the expt'l result of  $3.13 \pm 0.34 \cdot 10^{-3}$ . [Nico et al. (NIST), Nature, 2006]

The  $\mathcal{O}(1/M)$  terms contribute  $\mathcal{O}(0.04\%)$  to the Br.

# Beyond “V-A” in Neutron $\beta$ -Decay

The search for non-V-A interactions continues...

$$\begin{aligned}\mathcal{H}_{int} = & (\bar{\psi}_p \psi_n)(C_S \bar{\psi}_e \psi_\nu + C'_S \bar{\psi}_e \gamma_5 \psi_\nu) + (\bar{\psi}_p \gamma_\mu \psi_n)(C_V \bar{\psi}_e \gamma^\mu \psi_\nu + C'_V \bar{\psi}_e \gamma^\mu \gamma_5 \psi_\nu) \\ & - (\bar{\psi}_p \gamma_\mu \gamma_5 \psi_n)(C_A \bar{\psi}_e \gamma^\mu \gamma_5 \psi_\nu + C'_A \bar{\psi}_e \gamma^\mu \psi_\nu) + (\bar{\psi}_p \gamma_5 \gamma_\mu \psi_n)(C_P \bar{\psi}_e \gamma_5 \psi_\nu + C'_P \bar{\psi}_e \psi_\nu) \\ & + \frac{1}{2} (\bar{\psi}_p \sigma_{\lambda\mu} \psi_n)(C_T \bar{\psi}_e \sigma^{\lambda\mu} \psi_\nu + C'_T \bar{\psi}_e \sigma^{\lambda\mu} \gamma_5 \psi_\nu) + h.c.\end{aligned}$$

[Lee and Yang, 1956; note also Gamow and Teller, 1936]

$C'_X$  denote parity-nonconserving interactions.

In polarized neutron (nuclear)  $\beta$ -decay one more correlation appears:  $b$

$$\begin{aligned}d^3\Gamma = & \frac{1}{(2\pi)^5} \xi E_e |\mathbf{p}_e| (E_e^{\max} - E_e)^2 \times \\ & [1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m}{E_e} + \mathbf{P} \cdot (A \frac{\mathbf{p}_e}{E_e} + B \frac{\mathbf{p}_\nu}{E_\nu} + D \frac{\mathbf{p}_e \times \mathbf{p}_\nu}{E_e E_\nu})] dE_e d\Omega_e d\Omega_\nu\end{aligned}$$

[Jackson, Treiman, and Wyld, Phys. Rev. 106, 517 (1957)]

Note, e.g.,

$$b\xi = \pm 2\text{Re}[C_S C_V^* + C'_S C_V'^* + 3(C_T C_A^* + C'_T C_A'^*)]$$

If the electron polarization is also detected, more correlations enter.

Recent limits on  $b$  come from nuclear  $\beta$ -decay:

- $b = +0.0001 \pm 0.0026$  ( $|C_S/C_V| \leq 0.0013$ )  
from survey of  $0^+ \rightarrow 0^+$  transitions in nuclei

[Towner and Hardy, PRL 94, 092502 (2005)]

- $\tilde{a} \equiv a/(1 + bm_e/\langle E_e \rangle) = 0.9981 \pm 0.0030 \pm 0.0037$   
from  $0^+ \rightarrow 0^+$  pure Fermi decay of  $^{38m}\text{K}$

[A. Gorelov et al., PRL 94, 142501 (2005)]

Both limits are consistent with the Standard Model.

Tests to this precision do not rely on the knowledge of nuclear structure in any way.

Ingredients: CVC hypothesis ( $g_V = (1 + \mathcal{O}(\alpha))V_{ud}$ ), recoil expansion ( $\mathcal{O}(E)/M \ll 1$ ).

It is possible to test the CVC hypothesis (and more) in neutron  $\beta$ -decay through comparison of the  $a$  and  $A$  correlation coefficients. [SG, Zhang, PRL 2001]

# Global Fits to Neutron and Nuclear $\beta$ -Decay Data

A seven-parameter (real couplings) global fit yields

[Severijns, Beck, Naviliat-Cuncic, RMP, 2006]

$$-1.40 < C_A/C_V < -1.17$$

$$0.87 < C'_V/C_V < 1.17$$

$$0.86 < C'_A/C_A < 1.16$$

$$-0.065 < C_S/C_V < 0.070$$

$$-0.067 < C'_S/C_V < 0.066$$

$$-0.076 < C_T/C_A < 0.090$$

$$-0.078 < C'_T/C_A < 0.089$$

At 95.5% CL one encloses the SM, namely  $C_S = C'_S = C_T = C'_T = 0$  and  $C'_V/C_V = C'_A/C_A = 1$ .

How large do we expect new physics effects to be?

Let's look at the  $C_S$  term in  $\mathcal{H}_{int}$  in a quark basis e.g.:

$$C_S \bar{\psi}_p \psi_n \bar{\psi}_e \psi_\nu \rightarrow C_S^q \bar{\psi}_u \psi_d \bar{\psi}_e \psi_\nu$$

This is a dimension-6 operator, so that we'd expect

$$C_S^q \sim \frac{\alpha}{4\pi} \left( \frac{M_W}{M_{\text{new}}} \right)^2 \sim 10^{-3} \quad \text{if} \quad M_W \sim M_{\text{new}}$$

# The Emergence of Physics Beyond the Standard Model

Why do we think there is new physics at  $\sim 1$  TeV?

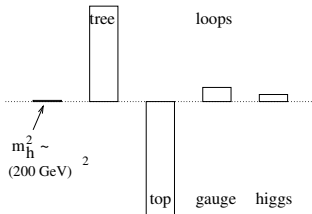
[Schmaltz, hep-ph/0210415]

Suppose we assume the Standard Model is valid for scales  $E \leq \Lambda$ , where  $\Lambda \sim \mathcal{O}(1\text{TeV})$ .

At one-loop level, we find large corrections to the tree-level Higgs mass  $m_{\text{tree}}$ .

All contributions must sum to  $m_H^2 \sim (200\text{GeV})^2$ , but each one  $\sim \Lambda^2$ !

At  $\Lambda = 10$  TeV,  $m_{\text{tree}}$  must be tuned to one part in 100!

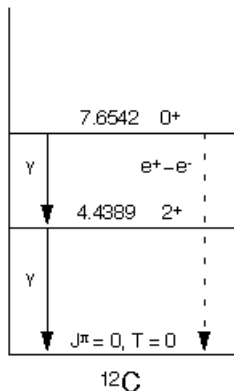


New physics at the TeV scale can enter to make the cancellations “natural.”

# “Fine-Tuning” does exist in Nature



$$\frac{7.2747}{3\alpha}$$



$$\frac{7.3666}{\alpha + {}^8\text{Be}}$$

[Hoyle, 1953; Cook, Fowler, Lauritsen, Lauritsen, 1957]

# The New Physics We Know...

We do have direct empirical evidence from terrestrial experiments for physics beyond the Standard Model.

Empirical evidence for neutrino oscillations allows us to conclude  $\Delta m^2 \equiv m_i^2 - m_j^2 \neq 0$  with surety.

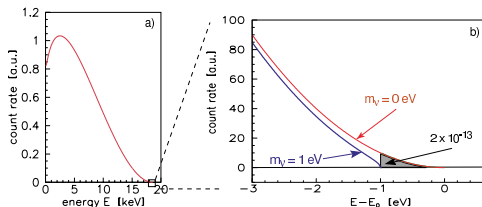
That is, neutrinos have mass.

This is not to say that the effects of neutrino mass are large.

Note  $m(\nu_e) \leq 2.3 \text{ eV}/c^2$  at 95% CL from  ${}^3\text{H}$   $\beta$ -decay [Ch. Kraus et al., EPJ C40 (2005) 447.] and  $\sum_\nu m(\nu) < 0.66 \text{ eV}/c^2$  at 95% CL from 3-year WMAP data set and others ( $\Lambda$ CDM Model).

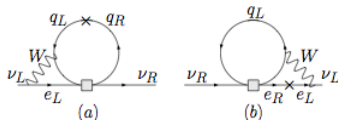
[D.N. Spergel et al. (WMAP), Astrophys. J. Suppl. 170 (2007) 377.]

Distortions in the shape of the electron energy spectrum in  ${}^3\text{H}$   $\beta$ -decay near its endpoint bound  $m_\nu^2$ . [KATRIN, loi]



## $\nu$ Mass Constraints on $\beta$ -Decay?

The  $\nu$  mass involves chirality-changing interactions, e.g.,



which can appear in other observables, such as the magnetic moment. Using “naturalness” bounds in an EFT framework yields for a Dirac neutrino,

$$\mu_\nu \lesssim 3 \cdot 10^{-15} \mu_B \left( \frac{m_\nu}{1 \text{ eV}} \right) \left( \frac{1 \text{ TeV}}{\Lambda} \right)^2$$

[N.F. Bell et al., PRL **95** (2005) 151802.]

Such relationships can be evaded, typically by imposing a symmetry which makes  $m_\nu$  “unnaturally” small. [Volshin, SJNP 1988; Georgi and Randall, PLB 1990; Grimus and Neufeld, NPB 1991; Babu and Mohapatra, PRL 1990; Barr, Freire, and Zee, PRL 1990.]

Similar ideas can be used to bound scalar and tensor interactions in  $\beta$  decay from chirality-changing operators.

[Ito and Prezeau, PRL 2005.]

Using CMB  $\nu$  mass bounds, yields, e.g.,

$$|C_S/C_V| \lesssim 5 \cdot 10^{-3}; |C_T/C_A| \lesssim 1.2 \cdot 10^{-2}$$

[Ito and Prezeau, PRL 2005.]

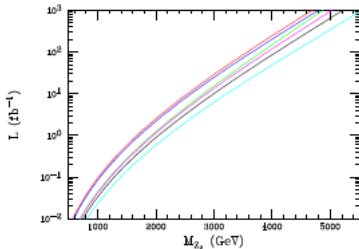
However, effective scalar and tensor couplings can be generated in other ways, note, e.g., and can be *much* larger.

[Profumo, Ramsey-Musolf, Tulin, 2006]

$\nu$  mass constraints aren't show-stoppers!

The Lesson of the  $Z'$ . Note  $5\sigma$  discovery reach:

The LHC should accumulate  $10\text{fb}^{-1}$  in  $L$  each year.



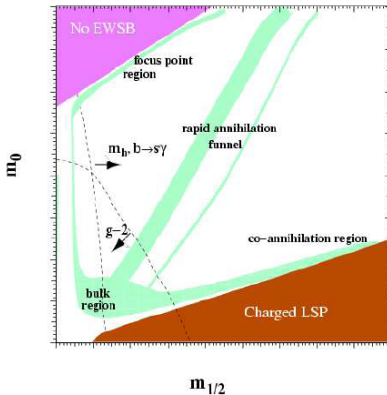
[T. Rizzo (SLAC), TASI 06]

The LHC should quickly find a  $Z'$  of a few TeV in mass — and eventually determine its spin.

But is it *really* a  $Z'$ ? For that, determining its couplings to SM fermions are essential... and low-energy experiments can play a crucial role.

# Complementarity

In supersymmetric models with restricted parameter space (note the “CMSSM”), the constraints of the superpartner masses from cosmological and low-energy data are severe. **Caveat Emptor!**



[M. Schmitt (Northwestern), SSI 2007, after J. Feng, astro-ph/0511043 and refs. therein]

Major ticks are separated by 100 GeV.

We look forward to an era of discovery!